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# THE UNITED STATES OF AMERICA

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April 11, 2003

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**APPLICATION NUMBER:** 60/363,139

**FILING DATE:** March 08, 2002

**RELATED PCT APPLICATION NUMBER:** PCT/US03/07123

By Authority of the  
COMMISSIONER OF PATENTS AND TRADEMARKS



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# PROVISIONAL APPLICATION FOR PATENT COVER SHEET

This is a request for filing a PROVISIONAL APPLICATION FOR PATENT under 37 CFR 1.53(c).

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10/11 U.S. PTO  
60/063139  
03/08/02

INVENTOR(S)					
Given Name (first and middle [if any])		Family Name or Surname		Residence (City and either State or Foreign Country)	
Mark N.		Horenstein		West Roxbury, MA 02132	
<input type="checkbox"/> Additional inventors are being named on the _____ separately numbered sheets attached hereto					
TITLE OF THE INVENTION (500 characters max)					
METHOD FOR LINEARIZING DEFLECTION OF A MEMS DEVICE USING BINARY ELECTRODES AND VOLTAGE MODULATION					
Direct correspondence to: CORRESPONDENCE ADDRESS					
<input checked="" type="checkbox"/> Customer Number		022383		Place Customer Number Bar Code Label here	
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ENCLOSED APPLICATION PARTS (check all that apply)					
<input checked="" type="checkbox"/> Specification		Number of Pages		6	
<input type="checkbox"/> Drawing(s)		Number of Sheets			
<input type="checkbox"/> Application Data Sheet. See 37 CFR 1.76		<input type="checkbox"/> CD(s), Number			
		<input type="checkbox"/> Other (specify)			
METHOD OF PAYMENT OF FILING FEES FOR THIS PROVISIONAL APPLICATION FOR PATENT					
<input checked="" type="checkbox"/> Applicant claims small entity status. See 37 CFR 1.27.				FILING FEE AMOUNT (\$)	
<input type="checkbox"/> A check or money order is enclosed to cover the filing fees					
<input checked="" type="checkbox"/> The Commissioner is hereby authorized to charge filing fees or credit any overpayment to Deposit Account Number:		023255		\$80.00	
<input type="checkbox"/> Payment by credit card. Form PTO-2038 is attached.					
The invention was made by an agency of the United States Government or under a contract with an agency of the United States Government.					
<input type="checkbox"/> No.					
<input type="checkbox"/> Yes, the name of the U.S. Government agency and the Government contract number are: _____					

Respectfully submitted,

SIGNATURE

*Mark N. Horenstein*

Date

03/08/2002

TYPED or PRINTED NAME

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REGISTRATION NO.

(if appropriate)

Docket Number:

BU02-15

TELEPHONE

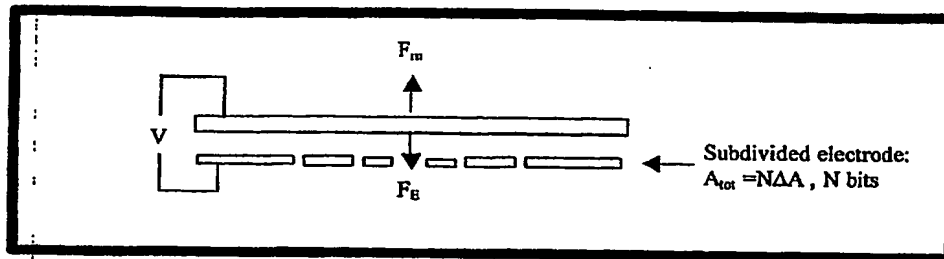
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## USE ONLY FOR FILING A PROVISIONAL APPLICATION FOR PATENT

This collection of information is required by 37 CFR 1.51. The information is used by the public to file (and by the PTO to process) a provisional application. Confidentiality is governed by 35 U.S.C. 122 and 37 CFR 1.14. This collection is estimated to take 8 hours to complete, including gathering, preparing, and submitting the complete provisional application to the PTO. Time will vary depending upon the individual case. Any comments on the amount of time you require to complete this form and/or suggestions for reducing this burden, should be sent to the Chief Information Officer, U.S. Patent and Trademark Office, U.S. Department of Commerce, Washington, D.C. 20231. DO NOT SEND FEES OR COMPLETED FORMS TO THIS ADDRESS. SEND TO: Box Provisional Application, Assistant Commissioner for Patents, Washington, D.C. 20231.

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Notes on Multi-Electrode System  
28 November 2001



Governing Equations

$$F_m = \frac{192EIx}{L^3}$$

Mechanical restoring force for a given displacement,  $x$

$$F_E = \frac{\epsilon AV^2}{2(g-x)^2}$$

Electrostatic Force

Equilibrium occurs when  $F_m = F_E$ :

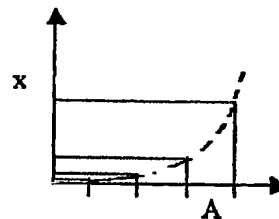
$$A = \frac{C}{V^2} x(g-x)^2 = \frac{C}{V^2} [x^3 - 2gx^2 + g^2x]$$

where,

$$C = \frac{384EI}{L^3 \epsilon}$$

**Problem:**

Deflection, " $x$ ", is a strongly non-linear function of area, " $A$ ". Therefore, actuation approach based on fixed voltage and uniform increments in  $A$  will not lead to uniform increments in phase.



Mathematically:

$$A = \frac{C}{V^2} x(g-x)^2 = \frac{C}{V^2} [x^3 - 2gx^2 + g^2x]$$

$$\frac{dA}{dx} = \frac{C}{V^2} [3x^2 - 4gx + g^2]$$

$$\text{so: } \frac{dx}{dA} = \frac{V^2}{C[3x^2 - 4gx + g^2]}$$

An estimate of the largest step in "x" made by uniformly increasing "A" is:

$$\Delta x_m = \left. \frac{dx}{dA} \right|_{x_m} \cdot \Delta A$$

where  $x_m$  in the maximum required value of x;  $\Delta x_m$  in the maximum x step.

$$\text{But: } \Delta A = \frac{A_{tot}}{2^n - 1} \quad \text{by design}$$

$$\text{And } A_{tot} = \frac{C}{V^2} x_m (g - x_m)^2 \quad \text{by model}$$

therefore

$$\Delta x_m = \frac{V^2 C x_m (g - x_m)^2}{C V^2 [2^n - 1] [3x_m^2 - 4gx_m + g^2]}$$

simplifying:

$$\frac{x_m}{\Delta x_m} = \frac{(2^n - 1)(g - 3x_m)}{(g - x_m)}$$

The resolution of the actuator can be defined as one part in M, where

$$M = \frac{x_m}{\Delta x_m}$$

$$\therefore M = \left( \frac{g - 3x_m}{g - x_m} \right) (2^n - 1)$$

Non-linearity is worst for  $g = 3x_m$ , and improves as  $g$  increases.

Example:

$$g = 3.1x_m$$

$$M = \left( \frac{0.1}{2.1} \right) (2^n - 1)$$

Factor of 20+ loss of resolution (e.g. 8 bit system provides ~3 bit resolution)

Resolution Reduction Factor, R is:

$$\frac{1}{R} = \left( \frac{g - 3x_m}{g - x_m} \right)$$

Improvement in resolution is possible, by increasing "g".

$g$	$R$	
$3.1x_m$	21	(~silicon single-gap structures)
$4x_m$	3	
$5x_m$	2	if $g \geq 5x_m$ , only 1 bit of resolution is lost silicon double-gap structures
$6.7x_m$	1.5	

Price: Increase driving voltage

$$V^2 = \frac{C}{A} x (g - x)^2$$

therefore:

$$\left( \frac{V_2}{V_1} \right)^2 = \frac{C/A x_m (g_m - x_m)^2}{C/A x_m (g_m - x_m)^2}$$

and

$$\frac{V_2}{V_1} = \frac{g_2 - x_2}{g_1 - x_1}$$

is the ratio of maximum required voltages for two different gaps.  $C, A$ , and  $x_m$  unchanged.

If  $g_2 = 5x_m$ , and  $g_1 = 3x_m$ ,

$$V_2 = 2V_1$$

### Alternative solution: Linearize

$$AV^2 = Cx(g-x)^2$$

this could be linearized by imposing the constraint that:

$$V^2 \propto (g-x)^2 \text{ or } V = k(g-x)$$

then  $A = \frac{C}{k^2} x$

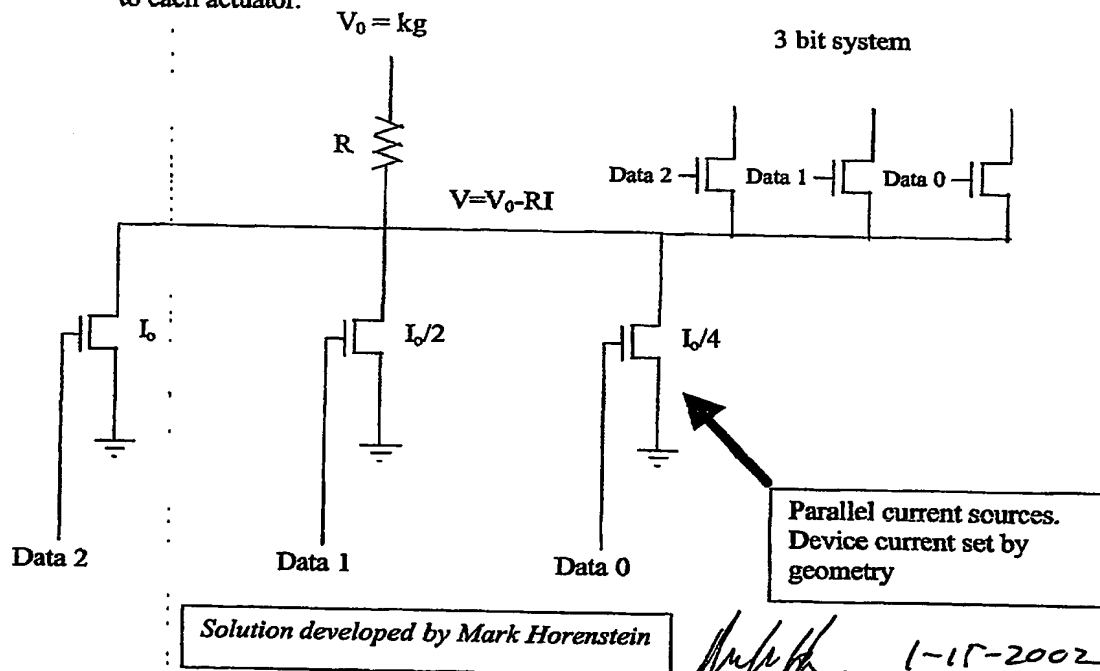
find value of k:

$$A_{tot} = \frac{C}{k^2} x_m \quad k = \sqrt{\frac{Cx_m}{A_{tot}}}$$

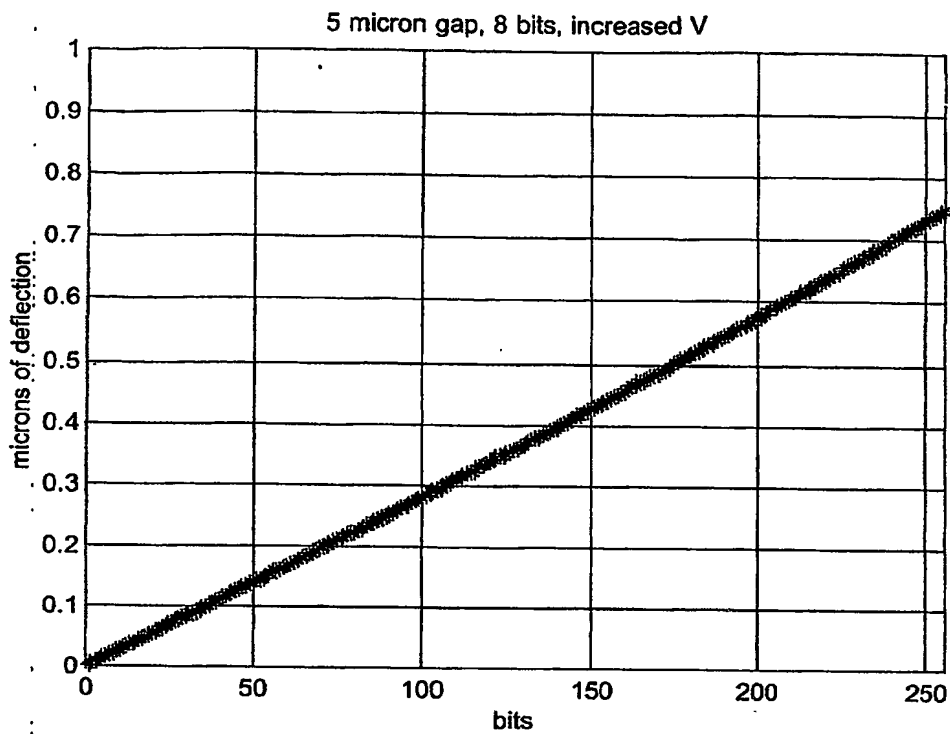
For the silicon structures with a 2.5  $\mu\text{m}$  gap:  $V_1 \sim 70\text{V}$  and  $V_f \sim 50\text{V}$

How to make  $V = k(g-x)$ ?

Input to system (binary) is a linear representation of x. Use the data bus to modify voltage to each actuator:



Model of an 8 bit system, with a 5  $\mu\text{m}$  gap using the linearized voltage solution ( $V_1 = 130\text{V}$ )



60353139.030802

bozo1

%--MATLAB PROGRAM--

%Example of linearizing the deflection versus digital input curve.

%Requires that the voltage applied to the electrodes be reduced as

%the digital input n goes up from 0 to N (where N = 16, 128, 256, etc)

close; clear; %close any previous plots and reset

variables

N=256;

%Maximum value of digital

input 2^n where n=0...N (8 bits in this example)

%elastic restoring force in

k = 60;

N/m (typical)

eo = 8.85e-12;

%electric permittivity of air

side = 250e-6;

%dimension of each side of actuator

Area = side^2;

%total area of actuator

Ao=Area/N;

%smallest increment of area

(area increment per digital bit)

gap = 5e-6;

%spacing between actuator and

activation electrode

dy = gap/1000;

%incremental deflection to be used

in iteration

for n=1:N;

%Plot y versus digital input

n for n=1...N:

V=40\*(1-n/(8\*N)); %V is a function of n. Equal to 40 V at start, decreases

%in a straight line

function with n. I think we can do this

%in a straightforward manner electronically in VLSI.

%----Iteration to solve for deflection y as a function of digital input n ----

y=0;

%initialize deflection to zero

Fm = k\*y;

%Compute magnitude of

mechanical force

Fe = eo\*Ao\*n\*V^2/(2\*(gap-y)^2);

%Compute magnitude of electrostatic force

%(Total area is n times Ao)

%-----

while Fm < Fe;

%Try a slightly larger

deflection

y = y + dy;

%Recompute magnitude of

mechanical force

Fm = k\*y;

Fe = eo\*Ao\*n\*V^2/(gap-y)^2;

%Recompute magnitude of electrostatic force

%Get

out of loop when Fm = Fe.

end

Y(n)=y;

%Save this value of y(n) for

later plotting

end

%Iterate over all

values of n from 0...N

%Done with iteration

plot(Y\*1e6)

%Plot deflection in microns

versus n

%Suggestions: variations on the program:

%Set V to a fixed 40 V; this change will demonstrate non-linearity in area vs n curve.

%Set V to 40\*(n/N) and change Ao\*n to Area; this change produces the usual nonlinear

%deflection versus voltage curve.